Homework #3 phy 5246 due: Friday, October 6 (in class)

Goldstein Poole, and Safko, Classical Mechanics (Third Edition) Chap. 2; Problem 14 Pg. 66. Chap. 2; Problem 18 Pg. 67. Chap. 2; Problem 23 Pg. 68.

P4: A particle of mass m is constrained to move under the influence of gravity on the surface of a paraboloid of revolution whose axis is vertical. Taking the z direction to be up, this surface is described by the equation

$$z = \alpha (x^2 + y^2) \quad \alpha > 0.$$

(a) Write the Lagrangian for this system using as generalized coordinates r and θ , the polar coordinates in the x - y plane.

(b) Reduce the problem to an effective one-dimensional problem for the radial coordinate r.

(c) Determine the condition on the particles initial velocity required to produce circular motion.

(d) Find the period of small oscillations about this circular motion.